

SIMULTANEOUS EQUATIONS - PRACTICE QUESTIONS



metatutor

1.

Solve the simultaneous equations:

$$2x + 5y = 9$$

$$- 2x + 3y = 7$$

$$\underline{\hspace{1cm}}$$
$$2y = 2$$

$$y = 1$$

$$2x + 3 \times 1 = 7$$

$$-3 \quad 2x + 3 = 7 \quad -3$$

$$\div 2 \quad 2x = 4 \quad \div 2$$

$$x = 2$$

$$\begin{matrix} y = 1 \\ x = 2 \end{matrix}$$

2.

Solve the simultaneous equations:

$$3x + 4y = 23$$

$$+ 2x - 4y = 2$$

$$\underline{\hspace{1cm}}$$
$$5x = 25$$

$$x = 5$$

$$3 \times 5 + 4y = 23$$

$$-15 \quad 15 + 4y = 23 \quad -15$$

$$\div 4 \quad 4y = 8 \quad \div 4$$

$$y = 2$$

$$\begin{matrix} x = 5 \\ y = 2 \end{matrix}$$

3.

Solve the simultaneous equations:

$$7x + 2y = 33$$

$$- 4x + 2y = 24$$

$$\underline{\hspace{1cm}}$$
$$3x = 9$$

$$x = 3$$

$$4 \times 3 + 2y = 24$$

$$-12 \quad 12 + 2y = 24 \quad -12$$

$$\div 2 \quad 2y = 12 \quad \div 2$$

$$y = 6$$

$$\begin{matrix} x = 3 \\ y = 6 \end{matrix}$$

4.

Solve the simultaneous equations:

$$\begin{array}{r} 10x + y = 29 \\ -7x + y = 20 \\ \hline 3x = 9 \\ x = 3 \end{array}$$

$$\begin{array}{r} 7 \times 3 + y = 20 \\ 21 + y = 20 \\ -21 \qquad \qquad -21 \\ \hline y = -1 \end{array}$$

$$\begin{array}{l} x = 3 \\ y = -1 \end{array}$$

5.

Solve the simultaneous equations:

$$\begin{array}{r} 3x + 2y = 17 \\ +5x - 2y = 7 \\ \hline 8x = 24 \\ x = 3 \end{array}$$

$$\begin{array}{r} 3 \times 3 + 2y = 17 \\ 9 + 2y = 17 \\ -9 \qquad \qquad -9 \\ \hline 2y = 8 \\ \div 2 \qquad \qquad \div 2 \\ y = 4 \end{array}$$

$$\begin{array}{l} x = 3 \\ y = 4 \end{array}$$

6.

Solve the simultaneous equations:

$$\begin{array}{r} 4x + 5y = 13 \\ -4x - 3y = 5 \\ \hline 8y = 8 \\ y = 1 \end{array}$$

$$\begin{array}{r} 4x + 5 \times 1 = 13 \\ 4x + 5 = 13 \\ -5 \qquad \qquad -5 \\ \hline 4x = 8 \\ \div 4 \qquad \qquad \div 4 \\ x = 2 \end{array}$$

$$\begin{array}{l} y = 1 \\ x = 2 \end{array}$$

7.

Solve the simultaneous equations:

$$\begin{array}{r} 3x + 5y = 19 \\ +7x - 5y = 11 \\ \hline 10x = 30 \\ x = 3 \end{array}$$

$$\begin{array}{r} 3 \times 3 + 5y = 19 \\ 9 + 5y = 19 \\ -9 \qquad \qquad -9 \\ \hline 5y = 10 \\ \div 5 \qquad \qquad \div 5 \\ y = 2 \end{array}$$

$$\begin{array}{l} x = 3 \\ y = 2 \end{array}$$

8.

Solve the simultaneous equations:

$$5x + 2y = 17$$

$$4x + y = 10 \quad \times 2 \quad 8x + 2y = 20$$

$$- \quad 5x + 2y = 17$$

$$\hline 3x = 3$$

$$x = 1$$

$$4 \times 1 + y = 10$$

$$4 + y = 10$$

$$-4 \quad -4$$
$$y = 6$$

$$x = 1$$
$$y = 6$$

9.

Solve the simultaneous equations:

$$6x + 5y = 13$$

$$2x + 3y = 3 \quad \times 3 \quad 6x + 9y = 9$$

$$- \quad 6x + 5y = 13$$

$$\hline 4y = -4$$

$$y = -1$$

$$2x + 3 \times -1 = 3$$

$$2x - 3 = 3$$

$$+3 \quad +3$$
$$\div 2 \quad \div 2$$
$$2x = 6$$

$$x = 3$$

$$y = -1$$
$$x = 3$$

10.

Solve the simultaneous equations:

$$3x + 2y = 23$$

$$4x - y = 16 \quad \times 2 \quad 8x - 2y = 32$$

$$+ \quad 3x + 2y = 23$$

$$\hline 11x = 55$$

$$x = 5$$

$$4 \times 5 - y = 16$$

$$20 - y = 16$$

$$y = 4$$

$$x = 5$$
$$y = 4$$

11.

Solve the simultaneous equations:

$$4x + 3y = 10 \quad \times 2 \quad 8x + 6y = 20$$

$$3x + 2y = 7 \quad \times 3 \quad 9x + 6y = 21$$

$$\underline{-8x + 6y = 20}$$

$$x = 1$$

$$3 \times 1 + 2y = 7$$

$$3 + 2y = 7$$

$$\begin{array}{r} -3 \\ 3 + 2y = 7 \\ -3 \end{array}$$

$$\begin{array}{r} \div 2 \\ 2y = 4 \\ \div 2 \end{array}$$

$$y = 2$$

$$\begin{array}{l} x = 1 \\ y = 2 \end{array}$$

12.

Solve the simultaneous equations:

$$3x + 5y = 14 \quad \times 2 \quad 6x + 10y = 28$$

$$2x + 3y = 9 \quad \times 3 \quad \underline{-6x + 9y = 27}$$

$$y = 1$$

$$2x + 3 \times 1 = 9$$

$$2x + 3 = 9$$

$$\begin{array}{r} -3 \\ 2x + 3 = 9 \\ -3 \end{array}$$

$$\begin{array}{r} \div 2 \\ 2x = 6 \\ \div 2 \end{array}$$

$$x = 3$$

$$\begin{array}{l} y = 1 \\ x = 3 \end{array}$$

13.

Solve the simultaneous equations:

$$3x + 4y = 11 \quad \times 3 \quad 9x + 12y = 33$$

$$7x - 3y = 1 \quad \times 4 \quad \underline{+28x - 12y = 4}$$

$$37x = 37$$

$$x = 1$$

$$3 \times 1 + 4y = 11$$

$$3 + 4y = 11$$

$$\begin{array}{r} -3 \\ 3 + 4y = 11 \\ -3 \end{array}$$

$$\begin{array}{r} \div 4 \\ 4y = 8 \\ \div 4 \end{array}$$

$$y = 2$$

$$\begin{array}{l} x = 1 \\ y = 2 \end{array}$$

14.

Solve the simultaneous equations:

$$\begin{array}{r} 7x + 3y = 27 \quad \times 2 \quad 14x + 6y = 54 \\ 3x - 2y = 5 \quad \times 3 \quad + 9x - 6y = 15 \\ \hline 23x = 69 \\ x = 3 \end{array}$$

$$\begin{array}{r} 7 \times 3 + 3y = 27 \\ 21 + 3y = 27 \\ -21 \quad -21 \\ \hline 3y = 6 \\ \div 3 \quad \div 3 \\ y = 2 \end{array}$$

$$\begin{array}{l} x = 3 \\ y = 2 \end{array}$$

15.

Solve the simultaneous equations:

$$\begin{array}{r} 5x + 6y = 13 \quad \times 2 \quad 10x + 12y = 26 \\ 3x + 4y = 8 \quad \times 3 \quad - 9x + 12y = 24 \\ \hline x = 2 \end{array}$$

$$\begin{array}{r} 3 \times 2 + 4y = 8 \\ 6 + 4y = 8 \\ -6 \quad -6 \\ \hline 4y = 2 \\ \div 4 \quad \div 4 \\ y = \frac{2}{4} \\ = \frac{1}{2} \end{array}$$

$$\begin{array}{l} x = 2 \\ y = \frac{1}{2} \end{array}$$

16.

Solve the simultaneous equations:

$$\begin{array}{r} 2x + 5y = 21 \quad \times 3 \quad 6x + 15y = 63 \\ 3x - 7y = 17 \quad \times 2 \quad - 6x - 14y = 34 \\ \hline 29y = 29 \\ y = 1 \end{array}$$

$$\begin{array}{r} 2x + 5 \times 1 = 21 \\ 2x + 5 = 21 \\ -5 \quad -5 \\ \hline 2x = 16 \\ \div 2 \quad \div 2 \\ x = 8 \end{array}$$

$$\begin{array}{l} y = 1 \\ x = 8 \end{array}$$

17.

Solve the simultaneous equations:

$$9x - 5y = 30$$

$$+ 2x + 5y = 25$$

$$\underline{11x = 55}$$

$$x = 5$$

$$2 \times 5 + 5y = 25$$

$$10 + 5y = 25$$

$$\begin{array}{r} -10 \\ \hline 5y = 15 \end{array}$$

$$\div 5 \quad \div 5$$

$$y = 3$$

$$\begin{array}{l} x = 5 \\ y = 3 \end{array}$$

18.

Solve the simultaneous equations:

$$5x + 8y = 19$$

$$3x + 4y = 9$$

$$\times 2 \quad 6x + 8y = 18$$

$$- 5x + 8y = 19$$

$$\underline{x = -1}$$

$$\begin{array}{l} x = -1 \\ y = 3 \end{array}$$

$$3x - 1 + 4y = 9$$

$$+3 \quad -3 + 4y = 9 \quad +3$$

$$+4 \quad 4y = 12 \quad \div 4$$

$$y = 3$$

19.

Solve the simultaneous equations:

$$8x - 3y = 12$$

$$3x + 2y = 17$$

$$\times 2 \quad 16x - 6y = 24$$

$$\times 3 \quad + 9x + 6y = 51$$

$$\underline{25x = 75}$$

$$x = 3$$

$$\begin{array}{l} x = 3 \\ y = 4 \end{array}$$

$$3 \times 3 + 2y = 17$$

$$-9 \quad 9 + 2y = 17 \quad -9$$

$$\div 2 \quad 2y = 8 \quad \div 2$$

$$y = 4$$

20.

Solve the simultaneous equations:

$$10x + 4y = 32$$

$$- 3x + 4y = 4$$

$$\underline{7x = 28}$$

$$x = 4$$

$$3 \times 4 + 4y = 4$$

$$12 + 4y = 4$$

$$\begin{array}{r} -12 \\ \hline 4y = -8 \end{array}$$

$$\div 4 \quad \div 4$$

$$y = -2$$

$$\begin{array}{l} x = 4 \\ y = -2 \end{array}$$

21.

Solve the simultaneous equations:

$$\begin{array}{r} 5x - 3y = 24 \quad \times 2 \\ 3x + 2y = 3 \quad \times 3 \end{array} \quad \begin{array}{r} 10x - 6y = 48 \\ + 9x + 6y = 9 \\ \hline \end{array}$$

$$19x = 57$$

$$x = 3$$

$$3 \times 3 + 2y = 3$$

$$9 + 2y = 3$$

-9

$$2y = -6$$

$$\div 2 \quad \div 2$$

$$y = -3$$

$$\begin{array}{l} x = 3 \\ y = -3 \end{array}$$

22.

Solve the simultaneous equations:

$$\begin{array}{r} 6x + 7y = 11 \quad \times 2 \\ 4x + 3y = 9 \quad \times 3 \end{array} \quad \begin{array}{r} 12x + 14y = 22 \\ - 12x + 9y = 27 \\ \hline \end{array}$$

$$5y = -5$$

$$y = -1$$

$$4x + 3 \times -1 = 9$$

$$4x - 3 = 9$$

+3

+3

$$\div 4 \quad 4x = 12$$

\div 4

$$x = 3$$

$$\begin{array}{l} y = -1 \\ x = 3 \end{array}$$

23.

Solve the simultaneous equations:

$$\begin{array}{r} 10x + 9y = 23 \\ 5x - 3y = 34 \quad \times 3 \end{array} \quad \begin{array}{r} 10x + 9y = 23 \\ + 15x - 9y = 102 \\ \hline \end{array}$$

$$25x = 125$$

$$x = 5$$

$$10 \times 5 + 9y = 23$$

$$50 + 9y = 23$$

-50

-50

$$\div 9 \quad 9y = -27 \quad \div 9$$

$$y = -3$$

$$\begin{array}{l} x = 5 \\ y = -3 \end{array}$$

24.

A café sells baguettes and sandwiches.

The first customer buys 3 baguettes and 4 sandwiches for £27.

The second customer buys 2 baguettes and 3 sandwiches for £19.

Find the cost of each item.

$$\begin{array}{r} 3b + 4s = 27 \quad \times 2 \\ 2b + 3s = 19 \quad \times 3 \\ \hline 6b + 8s = 54 \\ 6b + 9s = 57 \\ -6b + 8s = 54 \\ \hline s = 3 \end{array}$$

$$\begin{array}{r} 2b + 3 \times 3 = 19 \\ -9 \quad 2b + 9 = 19 \\ \hline 2b = 10 \\ \div 2 \quad b = 5 \end{array}$$

baguette = £5
sandwich = £3

25.

A grocer sells apples and bananas.

The cost of 3 apples and 4 bananas is £1.90.

The cost of 7 apples and 3 bananas is £2.85.

Find the cost of each item.

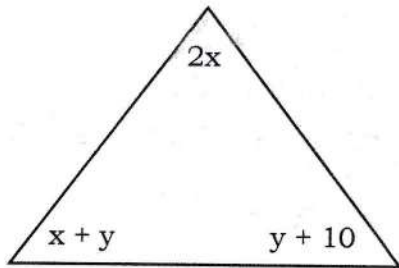
$$\begin{array}{r} 3a + 4b = 190 \quad \times 3 \\ 7a + 3b = 285 \quad \times 4 \\ \hline 9a + 12b = 570 \\ 28a + 12b = 1140 \\ -9a + 12b = 570 \\ \hline 19a = 570 \\ a = 30 \end{array}$$

$$\begin{array}{r} 3 \times 30 + 4b = 190 \\ -90 \quad 90 + 4b = 190 \\ \hline 4b = 100 \\ \div 4 \quad b = 25 \end{array}$$

apple = 30p
banana = 25p

26.

Find x and y .



$$\begin{aligned}2x + x + y + y + 10 &= 180 \\3x + 2y + 10 &= 180 \\3x + 2y &= 170\end{aligned}$$

$$3x + 2y = 170$$

$$5x - y = 175 \quad \times 2$$

$$\begin{aligned}10x - 2y &= 350 \\+ 3x + 2y &= 170\end{aligned}$$

$$13x = 520$$

$$x = 40$$

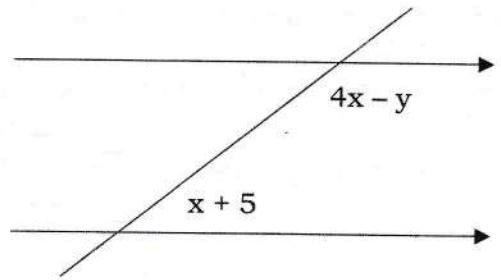
$$3 \times 40 + 2y = 170$$

$$120 + 2y = 170$$

$$2y = 50$$

$$y = 25$$

$$\begin{aligned}x &= 40^\circ \\y &= 25^\circ\end{aligned}$$



$$\begin{aligned}4x - y + x + 5 &= 180 \\5x - y + 5 &= 180 \\5x - y &= 175\end{aligned}$$

27.

50 tickets were sold for a concert.

Adult tickets cost £5 and child tickets cost £2.

The total money taken from the sale of the tickets was £160.

Find the number of child tickets sold and the number of adult tickets sold.

$$\begin{array}{r} 5a + 2c = 160 \\ a + c = 50 \quad \times 2 \quad - \quad \underline{2a + 2c = 100} \\ \hline 3a = 60 \\ a = 20 \end{array}$$

$$\begin{array}{r} 20 + c = 50 \\ c = 30 \end{array}$$

adult tickets = 20
child tickets = 30

28.

A football team played 35 games last season.

The team receives 3 points for a win, 1 point for a draw and no points for a loss.

The team lost 9 games and ended the season with 58 points.

Find how many wins and draws the team had last season.

$$35 - 9 = 26$$

$$\begin{array}{r} 3w + d = 58 \\ - \quad w + d = 26 \\ \hline 2w = 32 \\ w = 16 \end{array}$$

$$\begin{array}{r} 16 + d = 26 \\ d = 10 \end{array}$$

wins = 16
draws = 10